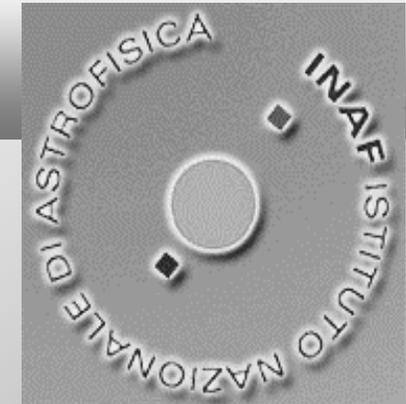


MULTI-TECHNIQUE APPROACH FOR DERIVING A VLBI SIGNAL EXTRA-PATH VARIATION MODEL INDUCED BY GRAVITY: THE EXAMPLE OF MEDICINA



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Overview

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- **Discrepancies** between **Tie vectors** and **SG solutions** are found in **TRF combinations**.
- Where do they originate from? (Deformations experienced by large VLBI antennas)
- How can these defs be modelled and handled?
- Application of a multi-technique procedure for estimating deformations parameters
- **Cross-check** of the results
- Formulation of a **Signal Path Variation Model** (valid for the Medicina VLBI telescope)

Inconsistencies between Ties & SG solutions

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- Inter-technique Combinations of SG solutions and tie vectors at co-located sites often point out remarkable inconsistencies
- Examples (**CATREF** combination residuals)

Combination	DOMES #	dN (mm)	dE (mm)	dU (mm)	Epoch
1	12711	1.2	-2.3	1.8	01:174
2	12711	0.1	-1.1	1	02:252
3	12711	1.5	-3.5	6.7	02:253
4	12711	0.2	0.6	0.6	03:274
5	12711	-0.8	1.6	5.7	06:194

- The way we compute **Tie vectors**
- **Reference Point Definition**

Reference Point: one or more?

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- A sort of “**trichotomy**” exists
 - 1. Electronic RP:** where the observable is detected and physically acquired (phase centres for GPS antenna and VLBI receivers)
 - 2. Conventional RP:** identified by the technique services according to a theoretical/geometrical definition (VLBI and SLR Invariant Point, GPS and DORIS Antenna Reference Point)
 - 3. Stochastic RP:** the outcome of an estimation procedure coming from either SG or terrestrial obs)

*Local ties don't have access to **Type No 1 of RP***

=> problem of **consistency** between the realization of RP with terrestrial and SG observable

The connection between the Electronic and Conventional RP

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- **Connection** between
Electronic & Conventional RP
GPS technique => PCV files (Schmidt et al 2005, 2007)
DORIS technique => (Willis et al 2007)
VLBI technique => need to consider similar corrections, due to Grav. Deformations

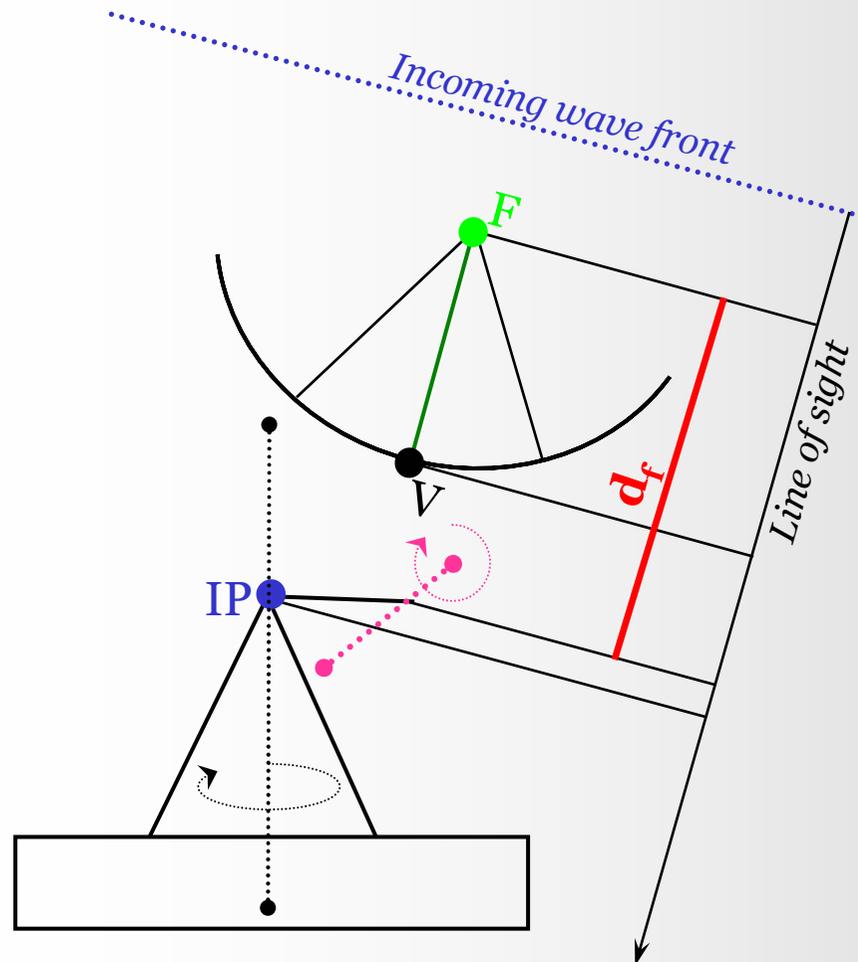
Indirect approach & Grav Deformations

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- **No unique way** to conventional RP realization:
*Direct, **Indirect**, Hybrid Approach (Sarti & Angermann, 2005)*
- **Flexibility** of indirect approaches
- Possibility to reconstruct the geometry of VLBI systems (axes, axis offset, IP)
- Contribution to the **understanding** of the effects of grav deformations
- ...but beware of indirect approaches! Handle with care!

Grav Deformations & Electronic RP instability

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- **Grav deformations** may induce Electronic RP (**F**) instabilities => reflect on the stability of **IP**
- In VLBI obs, **d_f** (*distance between **F** and moving axis*) is assumed to be **constant**
- *But...any variation in the signal path modifies **d_f***
- If **unmodelled**, this variation corrupts the observable and affects the parameters' estimations

Gravity dependent Signal Extra-path

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- ΔL *signal path variation* (referred to the **Line of Sight**)
- *Linear combination* of 3 contributions (Clark & Thomsen, 1988):

$$\Delta L = \alpha_f \Delta F + \alpha_v \Delta V + \alpha_R \Delta R$$

- the **3** α_i depend on the geometry of the VLBI telescope
- ΔL function of the antenna pointing elevation
- **Strictly peculiar** to the specific VLBI telescope

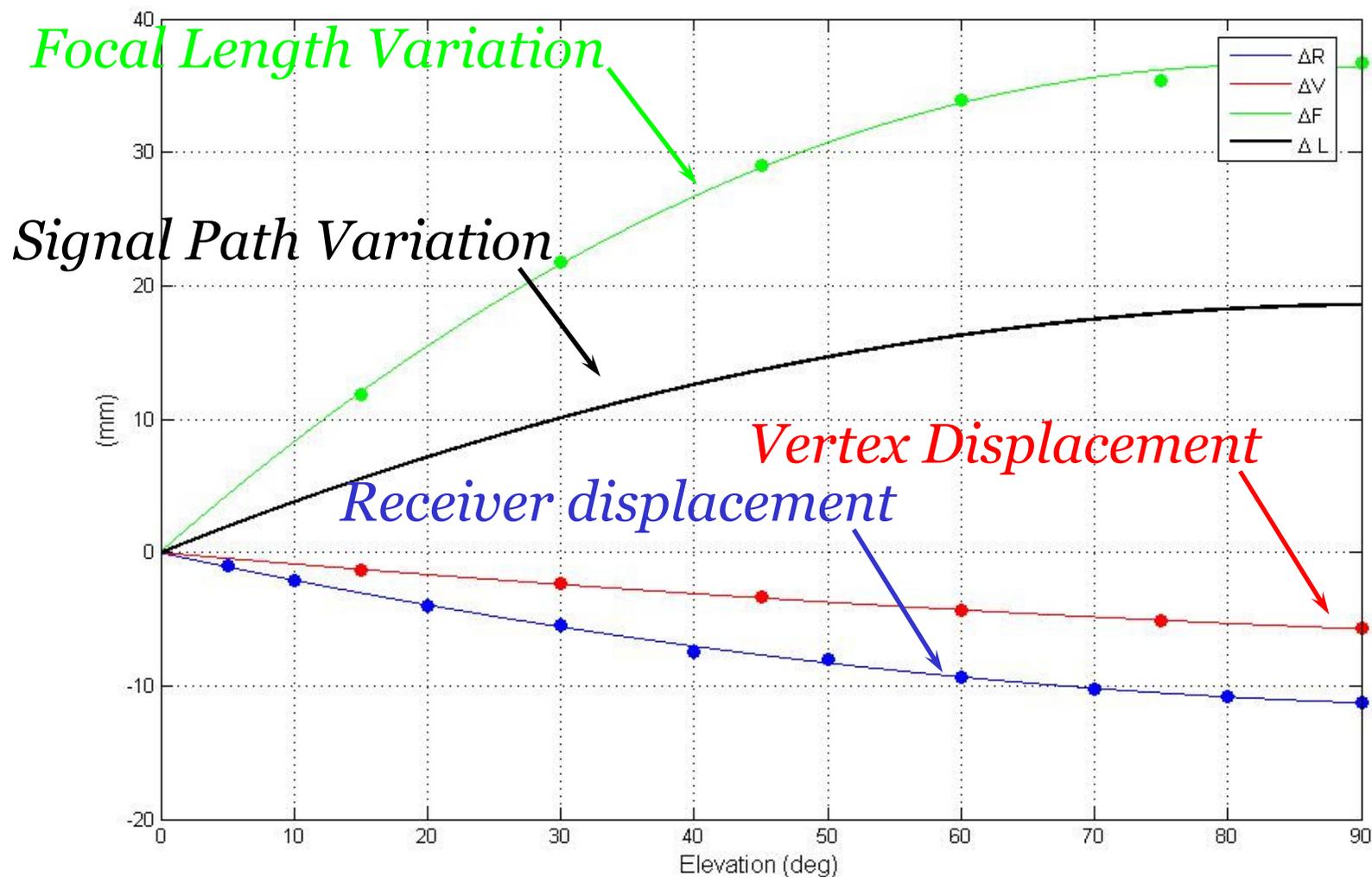
Quantifying the three effects

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- **Combination** of 3 methods (*Sarti et al. Submitted to JoG*):
- **Terrestrial Laser Scanning** on the primary reflector (**ΔF**) (*Sarti et al. 2009 in press JSE*)
- **Terrestrial Triangulation and Trilaterations** (**ΔR**)
- **Finite Element Modelling** (**ΔV**)

Signal Path Variation

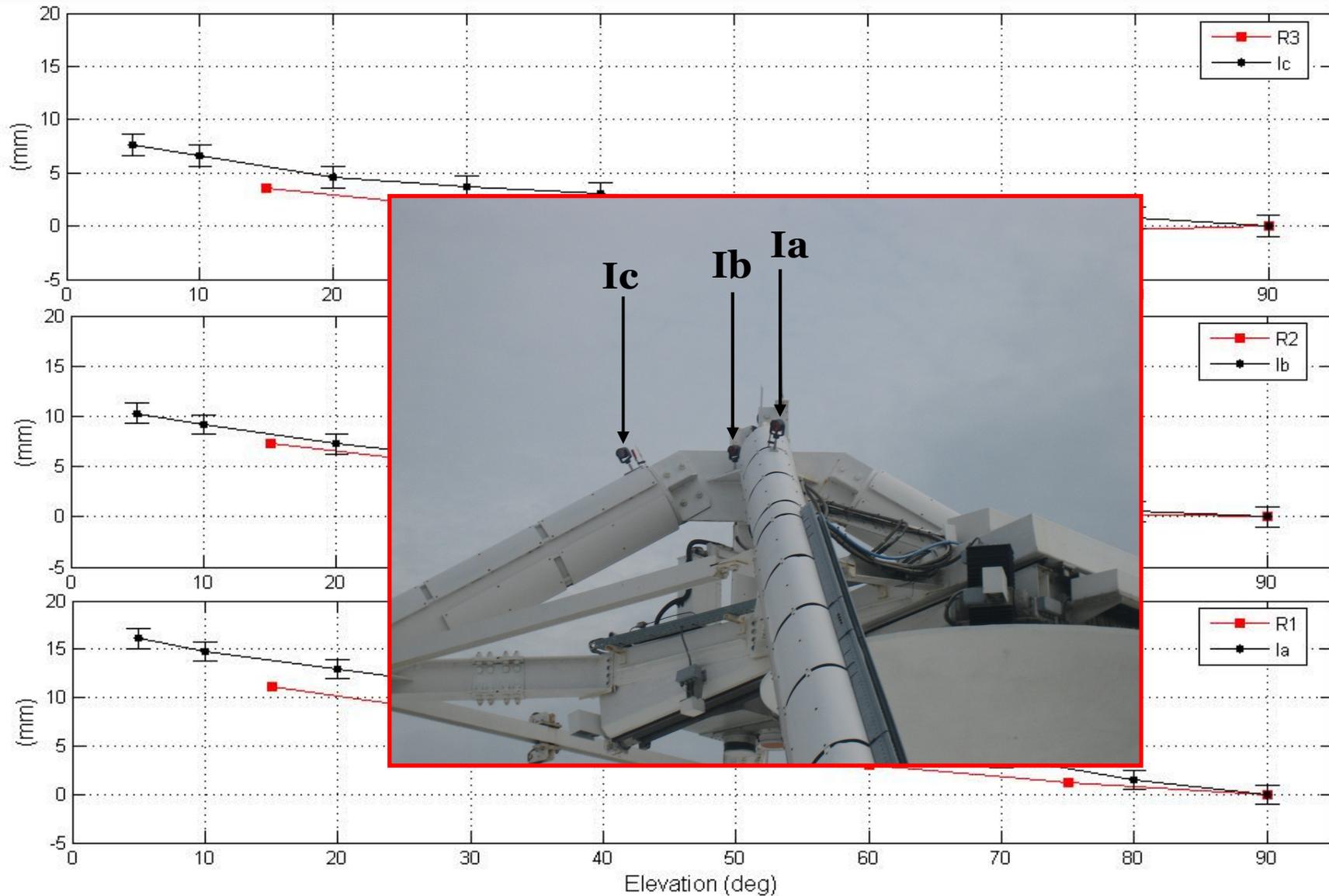
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Cross Check (1): The Receiver Motion (1)

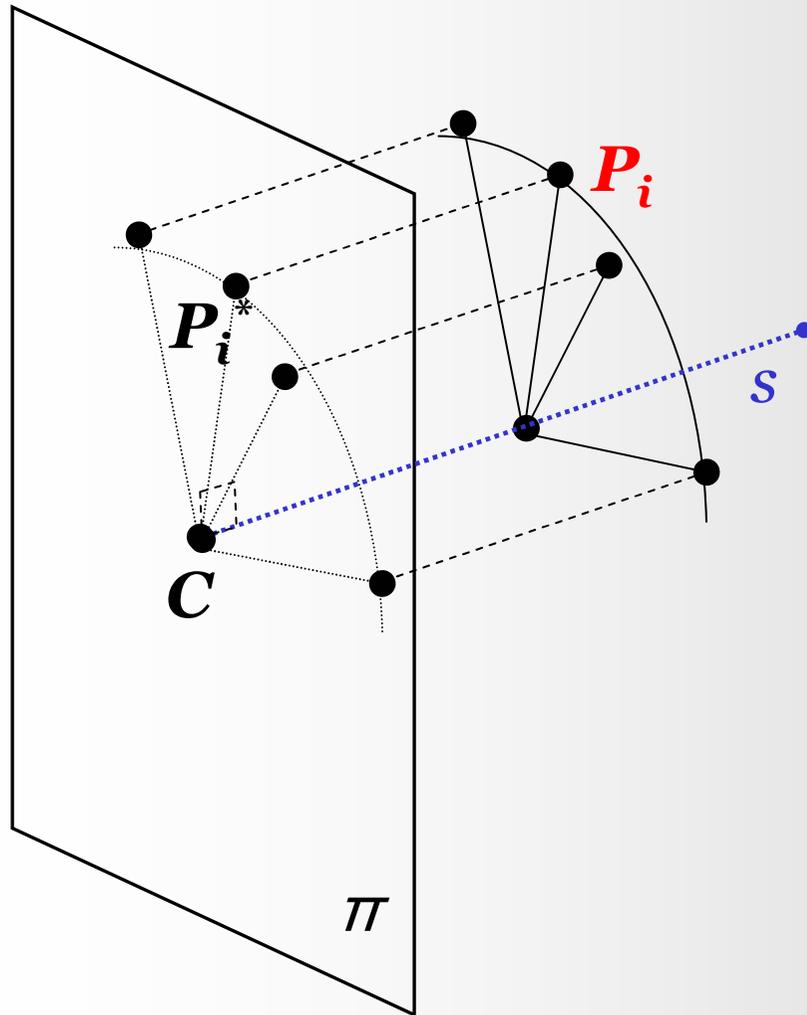
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Cross Check (1): The Receiver Motion (2)

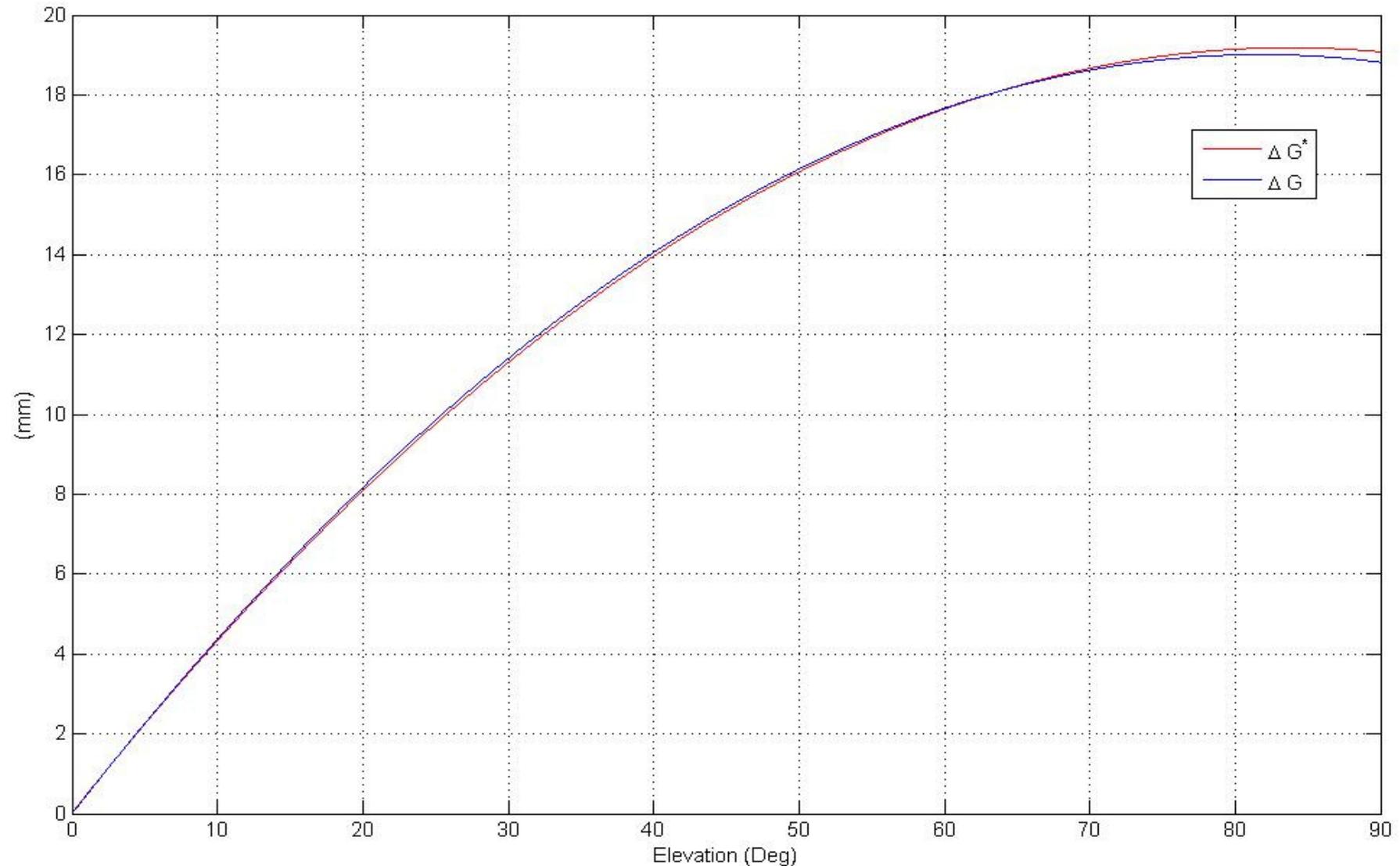
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- The graphs showed
- **Variations of radial distances** between
- **the elevation axis (s)** and the **targets P_i**
- Suitably projected onto a **reference plane** which is **orthogonal** to the **elevation axis** and contains the **Line of Sight**.

Cross check (2): Signal path variation

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Possible consequences

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- The signal path variation may introduce a non-negligible **error** in the VLBI obs equ
- Such a variation $\sin(e)$ ($R^2=0.99$)
- Likewise the sensitivity of height on an error on the obs equation behaves as a sin function (Ray et al. 2005)
- => The 2 effects are **highly correlated**. What does this imply? *More investigations...*
- Carter et al. (1980) compared the tie vector *Westford-Haystack* VLBI antennas with SG solution
- and observed a discrepancy in the *height component* of the *baseline Westford-Haystack* of **13 sin(e)** mm

Conclusions

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- It might be necessary to introduce ad-hoc ***PCV-like models*** accounting for ***VLBI IP motion*** induced by gravity deformations (on *large antennas*)
- ***More*** efforts must be done for evaluating the impacts of deformations ***within the VLBI data processing***
- ***Cross-checking*** of results proved to be valuable
- Modest impact of gravitational deformations for the next generation of (smaller) VLBI antennas

**Thank You
for
the attention**

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